

Here are the more notable corrections and changes made in the paperback edition of *Optically polarized atoms: understanding light–atom interactions*:

- Page v, first paragraph of Acknowledgments, “and Andrey Jarmola” → “Andrey Jarmola, and Kyle Beloy”
- Page 10, Eq. (2.7), write  $\mathbf{I}$  as vector:

$$\mathbf{I}^2 = I_x^2 + I_y^2 + I_z^2.$$

- Page 14, Eq. (2.20), divide by  $\hbar$ :

$$\boldsymbol{\mu} = -\mu_B (\mathbf{I} + 2\mathbf{s}) / \hbar.$$

- Page 26, Eq. (2.27), divide by  $\hbar$ :

$$\boldsymbol{\mu}_I = g_I \mu_N \mathbf{I} / \hbar,$$

- Page 26, last line: replace “can only support multipole moments of rank 2<sup>κ</sup>” with “can only support multipole moments of rank  $\kappa$ ”
- Page 44, in Eq. (3.69), replace “ $\psi'^{m_1} = \mathcal{D}_{m_1 m} \psi^m$ .” with “ $\psi'^{m_1} = \mathcal{D}_{m_1 m_2} \psi^{m_2}$ .”
- Page 44, in beginning of Eq. (3.70), replace “ $|\psi\rangle = \mathcal{D}^{-1} |\psi'\rangle$ ” with “ $|\psi\rangle = \mathcal{D}^{-1} |\psi'\rangle$ ”
- Page 56, Eq. (4.6), multiply by  $-\mu_B / \hbar$ :

$$\boldsymbol{\mu} = \boldsymbol{\mu}_L + \boldsymbol{\mu}_S = -\mu_B (g_L \mathbf{L} + g_S \mathbf{S}) / \hbar.$$

- Page 57, Eq. (4.7), multiply by  $-1$ :

$$\begin{aligned} \mu_J &= \mu_L \cos \alpha + \mu_S \cos \beta \\ &= -\mu_B \sqrt{L(L+1)} \cos \alpha - 2\mu_B \sqrt{S(S+1)} \cos \beta. \end{aligned}$$

- Page 57, Eq. (4.10), multiply by  $-1$ :

$$g_J = -\frac{\mu_J}{\mu_B} \frac{\hbar}{|\mathbf{J}|} = 1 + \frac{J(J+1) + S(S+1) - L(L+1)}{2J(J+1)}.$$

- Page 58, before Eq. (4.17), “since  $\langle \mathbf{F} \rangle = m_F \hbar \hat{\mathbf{z}}$ ” → “since for an eigenstate of  $F_z$ ,  $\langle \mathbf{F} \rangle = m_F \hbar \hat{\mathbf{z}}$ ,”
- Page 58, Eq. (4.17), multiply by  $\hat{\mathbf{z}}$ :

$$\langle \boldsymbol{\mu} \rangle = -g_F \mu_B m_F \hat{\mathbf{z}} = -g_J \mu_B \langle \mathbf{J} \rangle / \hbar,$$

- Page 68, last line of Eq. (4.62), add minus sign to third case:

$$= \delta_{m'm} \langle \xi J \| d \| \xi' J' \rangle \times \begin{cases} \frac{\sqrt{J^2 - m^2}}{\sqrt{J(2J+1)(2J-1)}} & \text{for } J' = J - 1 \\ \frac{m}{\sqrt{J(J+1)(2J+1)}} & \text{for } J' = J \\ -\frac{\sqrt{(J+1)^2 - m^2}}{\sqrt{(J+1)(2J+1)(2J+3)}} & \text{for } J' = J + 1 \\ 0 & \text{for } |J' - J| > 1 \text{ or } J = J' = 0. \end{cases}$$

- Page 69, Eq. (4.67), change first case from 1 to  $-1$ :

$$\frac{\alpha_2}{\alpha_0} = \begin{cases} -1 & \text{for } J' = J - 1 \\ \frac{2J-1}{J+1} & \text{for } J' = J \\ \frac{-J(2J-1)}{(J+1)(2J+3)} & \text{for } J' = J + 1. \end{cases}$$

- Page 86, footnote, “Bluhm et al. (1996)” → “Blum (1996)”
- Page 94, before, in, and following Eq. (5.49), and in Eq. (5.50), replace  $\Gamma$  with  $\hat{\Gamma}$
- Page 94, following Eq. (5.49), change to “Here  $\hat{\Gamma}$  is a diagonal matrix with the population decay rate of each state on the diagonal.”
- Page 94, last sentence before Sec. 5.6, “Bluhm et al. (1996)” → “Blum (1996)”
- Page 102, Eq. (5.78), change  $J$  to  $F$ :

$$\rho_{FF}(\theta, \phi) = \sqrt{\frac{4\pi}{2F+1}} \sum_{\kappa=0}^{2F} \sum_{q=-\kappa}^{\kappa} \langle FF\kappa 0 | FF \rangle \rho^{\kappa q} Y_{\kappa q}(\theta, \phi).$$

- Page 116, first paragraph of Sec. 6.3, “Bluhm et al. 1996” → “Blum 1996”
- Page 144, inline equation in last paragraph, divide by  $\hbar$ , to read “ $H_B = -\boldsymbol{\mu} \cdot \mathbf{B} = \mu_B(\mathbf{L} + 2\mathbf{S}) \cdot \mathbf{B}/\hbar$ ”
- Page 149, first partial paragraph: “and  $\mu$  is the intrinsic magnetic moment” → “and  $\boldsymbol{\mu}$  is the intrinsic magnetic moment”
- Page 201, move “where we have used Eq. (7.62) with  $\Gamma = 1/\tau$ .” from after Eq. (10.58d) to after Eq. (10.59d), and swap the period and comma at the ends of Eqs. (10.58d) and (10.59d)
- Page 228, before Sec. 11.6, replace “Grossetete (1965)” with “Grossetête (1964)”.
- Page 326, insert “(From Acosta et al. 2008.)” at the beginning of Fig. 18.14 caption

- Page 329, Eq. (19.1), change to

$$\Delta E_{\xi J m} = \frac{\mathcal{E}_0^2}{4} \sum_{\xi' J' m'} \langle \xi J m | d_i | \xi' J' m' \rangle \langle \xi' J' m' | d_j | \xi J m \rangle \times \left( \frac{\varepsilon_i \varepsilon_j^*}{E_{\xi J m} - E_{\xi' J' m'} - \hbar\omega} + \frac{\varepsilon_i^* \varepsilon_j}{E_{\xi J m} - E_{\xi' J' m'} + \hbar\omega} \right),$$

- Page 331, Eq. (19.8), change angle brackets to absolute value:

$$\Delta E_{\xi J m} = \mathcal{E}_0^2 \left[ C_0 + C_1 m V_z + C_2 \left( m^2 - \frac{J(J+1)}{3} \right) \left( |\varepsilon_z|^2 - \frac{1}{3} \right) \right].$$

- Page 331, replace passage

It is convenient to define AC-Stark polarizabilities  $\alpha_k$  in terms of the  $C_k$  so that  $\alpha_0$  and  $\alpha_2$  are consistent with the usual definitions for static electric polarizabilities as given by Eq. (4.65).

When extrapolating from low-frequency polarizabilities to static polarizabilities, it is important to take into account the discontinuity related to the fact that the time-averaged value of the square of an oscillating field is one-half of the amplitude squared, and this factor of one-half is absent for a static field.

The second-rank tensor polarizability is defined so that the tensor shift averaged over  $m$  is zero and also, if the electric field is applied along  $\hat{\mathbf{z}}$ , then the tensor shift of the stretched states  $m = \pm J$  is  $-\alpha_2 \mathcal{E}_0^2$ . We adopt a similar convention for the vector term in the AC-Stark case: the vector shift of the  $m = J$  state for left circularly polarized light propagating along  $\hat{\mathbf{z}}$  is  $-\alpha_1 \mathcal{E}_0^2/2$ . This leads to the expression:

with

The parameters  $C_k$  are often written in terms of the AC-Stark polarizabilities  $\alpha_k$ , commonly defined so that the scalar and tensor AC polarizabilities,  $\alpha_0$  and  $\alpha_2$ , become equal to the corresponding static polarizabilities in the limit of a very-low-frequency linearly polarized field. In making this correspondence, we must remember that the AC-Stark shift is the average shift over an oscillation cycle of the electric field. Thus a low-frequency oscillating field of amplitude  $\mathcal{E}_0$  will produce an average AC shift that is one-half as large as the DC shift due to a static field  $\mathcal{E}_{\text{static}} = \mathcal{E}_0$ , since the average of the square of the oscillating field is  $\overline{\mathcal{E}^2} = \mathcal{E}_0^2/2$ .

Comparing with the definitions for the static electric polarizabilities as given by Eq. (4.65), and including the factor of one-half, we find that the AC scalar shift should be given by  $-\alpha_0 \mathcal{E}_0^2/4$ , while the value of  $\alpha_2$  can be specified by fixing the AC tensor shift as  $-\alpha_2 \mathcal{E}_0^2/4$  for the stretched states  $m = \pm J$  in the special case of a field linearly

polarized along  $\hat{\mathbf{z}}$ . Since there is no vector polarizability in the limit of a static field, its definition is somewhat arbitrary; a commonly used convention is that the vector shift of the  $m = J$  state for left circularly polarized light propagating along  $\hat{\mathbf{z}}$  is given by  $-\alpha_1 \mathcal{E}_0^2/8$ . (Note that some variation in the literature may be encountered in the definitions of  $\alpha_0$  and  $\alpha_2$ , as well as in the definition of  $\alpha_1$ .) Using these definitions, we have the expression:

- Page 331, Eq. (19.9), add a prefactor of 1/2, and an additional factor of 1/2 to the second term:

$$\Delta E_{\xi J m} = -\frac{\mathcal{E}_0^2}{4} \left( \alpha_0 + i\alpha_1 \frac{m}{2J} V_z + \alpha_2 \frac{3m^2 - J(J+1)}{J(2J-1)} \frac{3|\varepsilon_z|^2 - 1}{2} \right).$$

- Page 341, Table A.2, after line “ $R$  classical rotation operator” add line “ $R$  classical rotation matrix”
- Page 350, in Eqs. (D.38), (D.39) (twice), (D.40), and between Eqs. (D.38) and (D.39), replace “ $\tilde{R}$ ” with “ $\tilde{R}$ ”
- Page 355, replace period at the end of Eq. (E.16) with comma
- Page 359, 3rd line, “different density matrix then” → “different density matrix than”
- Page 360, replace reference

Acosta, V., Ledbetter, M. P., Rochester, S. M., Budker, D., Jackson-Kimball, D. F., Hovde, D. C., Gawlik, W., Pustelny, S. and Zachorowski, J. (2006). *Physical Review A*, **73**, 053404.

with

Acosta, V., Ledbetter, M. P., Rochester, S. M., Budker, D., Jackson Kimball, D. F., Hovde, D. C., Gawlik, W., Pustelny, S., Zachorowski, J. and Yashchuk, V. V. (2006). *Physical Review A*, **73**, 053404.

- Page 361, add new reference between Bluhm, R. and Blushs, K.:  
Blum, K. (1996). *Density Matrix Theory and Applications*. Physics of Atoms and Molecules, Plenum Press, New York, 2nd ed.
- Page 361, replace reference Balabas, M.V. et al. with  
Balabas, M. V., Karaulanov, T., Ledbetter, M. P. and Budker, D. (2010). *Physical Review Letters*, **105**, 070801.
- Page 363, replace pair of references

Ducloy, M. (1973). *Physical Review A*, **8**, 1844.

——— (1976). *Journal of Physics B*, **9**, 357.

with

Ducloy, M. (1976). *Journal of Physics B*, **9**, 357.

Ducloy, M., Gorza, M. P. and Decomps, B. (1973). *Optics Communications*, **8**, 21.

- Page 364, replace reference

Grossetete, F. (1965). *Journal de Physique*, **26**, 26.

with

Grossetête, F. (1964). *Journal de Physique*, **25**, 383.

- Page 367, replace reference

Yashchuk, V., Budker, D. and Zolotorev, M. (1999). *Trapped Charged Particles and Fundamental Physics*, Asilomar, CA, USA, *AIP Conf. Proc.*, vol. 457, pp. 177–81.

with

Yashchuk, V., Budker, D. and Zolotorev, M. (1999). D. Dubin and D. Schneider (eds.), *Trapped Charged Particles and Fundamental Physics*, American Institute of Physics, Asilomar, CA, USA, *AIP Conference Proceedings*, vol. 457, pp. 177–81.